



Article

# Optimal Parameter Identification of Single-Sensor Fractional Maximum Power Point Tracker for Thermoelectric Generator

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Abstract: A thermoelectric generator (TEG) is used for converting temperature difference and into DC directly to electric energy based on the Seebeck effect. This new technology has attracted researchers of sustainable energy. The energy obtained from the TEG depends on the temperature difference between the two sides of the TEG. A reliable MPP "maximum power point" tracker (MPPT) is mandatory to guarantee that the TEG is working close to the MPP under different operational conditions. There are two common methods that have been widely used to track the MPP: hill climbing (HC) and incremental conductance (INR). The HC method is very fast in tracking the MPP; however, oscillation can occur under a high steady state. On the contrary, the INR method needs more time to track the MPP but does not oscillate around the MPP. To overcome these issues, fractional control is adopted. Furthermore, the proposed MPPT requires only a single current sensor, as opposed to conventional MPPTs, which require at least two sensors: current and voltage sensors. The cost of the control system is reduced when the number of sensors is reduced. Hunger games search optimization is used to estimate the parameters of a single sensor optimized fractional MPPT (OFMPPT). During the optimization process, three parameters were assigned as decision variables: proportional gain, integral gain, and order, with the objective function being the TEG's energy. The results demonstrated the superiority of OFMPPT in both transient and steady state compared to HC and INR.

Keywords: thermoelectric generator; single sensor; MPPT; fractional control



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### 1. Introduction

The rapid advancement of fossil fuel utilization has resulted in significant environmental consequences, which are evident in abnormal climate change [1,2]. Various methods for controlling climate change have been developed, including: (1) increasing the efficiency of current processes through heat recovery [3,4], especially in energy intensive consuming industries [5,6]; (2) using efficient and environmentally friendly energy conversion devices such as fuel cells [7,8]; (3) and/or relying on sustainable renewable energy sources with low or no environmental impacts [9,10]. In the current stage, waste heat recovery is the most credible solution until commercial renewable energy sources are developed at reasonable prices compared to those of conventional fuels. Significant advances in waste heat recovery have recently been made [11,12]. Thermoelectric generators are used to convert

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temperature differences and direct current to electric energy using the Seebeck effect. The improved materials and geometry of the thermoelectric generator of the thermoelectric generator (TEG) have increased its efficiency [13]. Many thermoelectric materials are being explored for power generation applications, such as GeTe [14], PbTe [15],  $Bi_2Te_{3-x}Se_x$  [16],  $Bi_2Te_3$  [17], and silicides [18]. Despite this, TEG efficiency is low. Additional developments and efforts are still necessary to improve the TEG's performance. One possible solution for increasing TEG efficiency is the development of novel materials. The obtained TEG energy is primarily determined by the temperature difference between the two sides of the TEG. A second approach is to increase its harvested energy by employing maximum power point (MPP) trackers (MPPTs) [19]. MPPTs are now essential components in the construction of a low-cost TEG power source. MPPT control is typically accomplished through the use of DC–DC converters [20]. Based on the maximum power theorem, the MPPT forces the TEG to work near the MPP by adjusting the load to be balanced by the TEG's internal resistance [20].

Various MPPTs for TEG systems have been discovered in the literature, ranging from traditional techniques to modern intelligent techniques [21,22]. The hill climbing (HC) method has previously been the most frequently used for photovoltaic or TEG systems [21]. Although the HC MPPT can rapidly reach the MPP, it oscillates around the MPP at steady state conditions. On the other hand, the incremental resistance (INR), under steady state conditions, has a slow dynamic performance but no oscillations around the MPP. The fundamental idea behind the INR MPPT is that the power–current derivative is zero at MPP. Because the error signal is very small around the MPP, the INR step size is chosen according to the error signal to reduce steady state oscillations. An integrator is used to model the INR in this case, and the error signal is fed into the integrator input [23].

Recently, fractional control has been used in a variety of scientific and engineering fields. The fractional order is commonly used to improve controller performance in both linear and nonlinear systems (closed-loop). The "fractional order control" (FOC) method is based on the fractional calculus principle. Because of its advantages, the FOC is desired compared with the integer order control method [24]. Compared to integer-order control, fractional control is flexible in design and has demonstrated superior results [25]. As a result, fractional control has been used to improve the performance of conventional INR by replacing the discrete integrator with a discrete fractional PI controller. To increase the performance of optimized fraction MPPT, three main parameters must be defined correctly: integration gain (KI), proportional gain (KP), and fraction order ( $\lambda$ ).

Reducing the number of required sensors for tracking the MPP, on the other hand, reduces the cost of the controller. Most MPPTs require at least two [26,27] or three [28] sensors for TEG applications: a current sensor, a voltage sensor, and a temperature sensor. Park et al. [28] proposed a TEG MPPT that employs three sensors: two temperature sensors and one voltage sensor. This will raise the cost of the control system. As a result, the goal of this paper is to address all of the issues mentioned above in one configuration: improving transit response, eliminating oscillation around the MPP, and reducing the number of sensors. To accomplish this, the hunger games search (HGS) optimization algorithm was used to determine the best parameters for single-sensor optimized fractional MPPT (OFMPPT). The KI, KP, and  $\lambda$  are used as decision variables during the parameter identification process, whereas the harvested energy from the TEG is the objective function that must be maximized.

The main contributions of the paper can be outlined as follows.

- ✓ For first time, a single-sensor MPPT has been applied with a TEG power source;
- ✓ Optimal parameters of OFMPPT have been defined using hunger games search optimization;
- ✓ Reduction in the number of sensors;
- ✓ Steady state and dynamic tracking responses are improved simultaneously.

The second section describes the TEG power system. MPPTs with a single sensor have been examined in Section 3. Section 4 defines the procedure for identifying OFMPPT

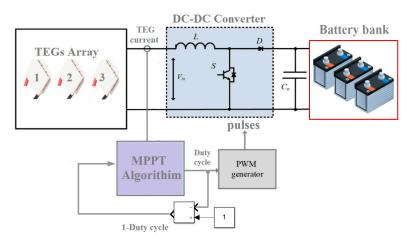
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parameters using hunger games search optimization. Section 5 contains a discussion and presentation of the results. Section 6 provides a summary of the primary findings.

#### 2. TEG's Power Conversion System

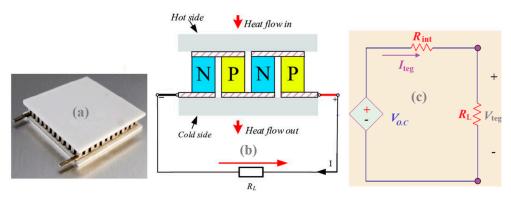
The power conversion process for the TEG system is shown in Figure 1. It has a battery bank, a boost DC–DC converter, an MPPT controller, and a TEGs array. The boost DC–DC converter takes the low output voltage of the TEG array and raises it to an appropriate DC voltage level that can be used by the battery bank or the DC link. In addition to this, it is responsible for maximizing the energy that can be harvested from the TEG by using an MPPT algorithm to update the duty cycle (D) so that it corresponds to the MPP [21]. As shown in the following equation, the output voltage of the boost converter, which represents the voltage of the battery ( $V_b$ ), is correlated to the input voltage, which represents the voltage of the TEG ( $V_{teg}$ ).

$$V_b = \frac{1}{1 - D} \times V_{teg} \tag{1}$$



**Figure 1.** TEG system's power stage with the suggested MPPT controller.

The TEG is a semiconductor device that generates a DC voltage via the Seebeck effect. Figure 2a depicts the common TEG view. As seen in Figure 2b, the TEG's basic unit is a thermocouple made up of n-type and p-type semiconductors. The p-type and n-type units are coupled in series to increase the output voltage. To reduce thermal resistance, the p-type and n-type units are thermally coupled in parallel [28] and the units are sandwiched between two ceramic sheets to form hot and cold sides. To form cold and hot sides, the units are sandwiched among two ceramic sheets.



**Figure 2.** (a) General overview of TEG, (b) P-type and N-type groups, and (c) simple equivalent-circuit of the TEG.

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When a temperature variance appears between the two sides of the TEG, the Seebeck effect generates a DC voltage. Figure 2c depicts a simple equivalent-circuit of the TEG. The open-circuit voltage is primarily determined by the difference in temperature between the cold and hot parts, and this can be calculated as follows:

$$V_{O\cdot C} = \alpha_{sh}(T_{hot} - T_{cold}) = \alpha_{sh} \cdot \Delta T \tag{2}$$

where  $\alpha_{sb}$  is the Seebeck coefficient

 $T_{hot}$  is the cold side temperature

 $T_{cold}$  is the hot side temperature

Heat flow from the high-temperature side  $(Q_h)$  to the low-temperature side  $(Q_c)$  can be estimated using the heat–energy equilibrium theory [27] in the following way:

$$Q_h = \alpha_{sb} I_{teg} T_{hot} + K\Delta T - 0.5 I_{teg}^2 R_{int}$$
(3)

$$Q_c = \alpha_{sb}I_{teg}T_{cold} + K\Delta T + 0.5I_{teg}^2R_{int}$$
(4)

where the thermal conductivity coefficient is K. To a large extent, the TEG output power,  $P_{teg}$ , is determined by the temperature difference between the two sides of the TEG. The following equation can be used to determine this value:

$$P_{teg} = Q_h - Q_c = (\alpha_{sb} \cdot \Delta T - I_{teg} R_{int}) I_{teg} = V_{teg} I_{teg}$$
(5)

based on Figure 2, and using KVL, a formula for the voltage produced by the TEG,  $V_{teg}$ , could be written as follows:

$$V_{teg} = \alpha_{sb} \cdot \Delta T - I_{teg} R_{int} = V_{O \cdot C} - I_{teg} R_{int} = I_{teg} R_L$$
 (6)

To summarize,  $P_{teg}$  is expressed as follows:

$$P_{teg} = (\alpha_{sb} \cdot \Delta T)^2 \frac{R_L}{(R_L + R_{int})^2} \tag{7}$$

#### 3. Single-Sensor MPPTs

As previously stated, most MPPTs used to track the MPP of the TEG require at least two or three sensors: a current sensor, a voltage sensor, and possibly a temperature sensor. According to Equation (1), the TEG voltage is proportional to (1-D) under constant battery voltage or DC-link voltage in DC grids. As a result, rather than using a voltage sensor, the value (1-D) can be used to substitute the TEG voltage. As a result, this concept has been implemented in this work. Three MPPT strategies, including incremental resistance, hill climbing, and optimized fractional MPPT, are examined.

# 3.1. Hill Climbing MPPT

The main HC-MPPT's benefit is that it is easy to implement. HC-MPPT has been used in a wide variety of contexts and is therefore very common. During the tracking process, HC adjusts the boost converter's duty cycle [21]. The Matlab model of HC-MPPT combined with the TEG and boost converter is shown in Figure 3. TEG current is measured and multiplied with (1-D) to obtain the objective function required to be maximum. Based on the change in the objective function, the duty cycle will be revised, raising the duty cycle with positive change in the objective function. On the other hand, by reducing the duty cycle with a negative change in the objective function, the main drawback of HC-MPPT is that it exhibits significant oscillations around the MPP in steady state conditions.

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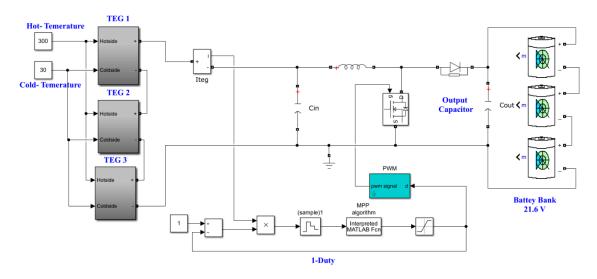


Figure 3. Matlab model of single-sensor HC-MPPT.

# 3.2. Incremental Resistance MPPT

The INR-MPPT is based on the fact that the derivative of the power over current (dP/dI) is zero at MPP. Further details regarding INR-MPPT can be found in [23]. Considering that the TEG voltage is proportional with (1 - D), the error signal e(t) could be estimated by the following relations.

$$\frac{dp}{dI}@MPP = \frac{d(V \times I)}{dI} = \frac{d([1 - D] \times I)}{dI} = [1 - D] + I\frac{d[1 - D]}{dI} = 0,$$
(8)

$$\frac{d[1-D]}{dI} + \frac{[1-D]}{I} = \frac{[1-D](t) - [1-D](t-1)}{I(t) - I(t-1)} + \frac{[1-D](t)}{I(t)} = 0.$$
 (9)

Moreover,

$$e(t) = \frac{[1-D](t) - [1-D](t-1)}{I(t) - I(t-1)} + \frac{[1-D](t)}{I(t)}.$$
 (10)

Because e(t), or "the error signal", is small in the vicinity of the MPP, the steady state oscillations can be reduced by adjusting the step size of the INR-MPPT. A discrete time integrator (DTI), as described in Figure 4, is used to accomplish this modeling of the INR-MPPT. The error signal is used as DTI's input.

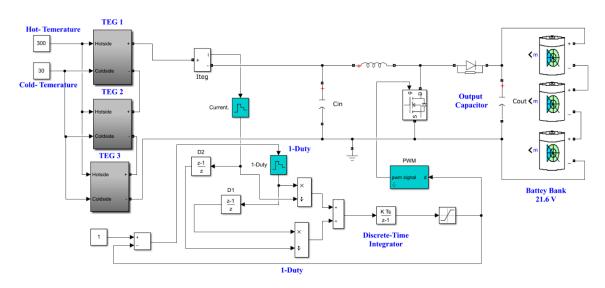


Figure 4. Matlab model of single-sensor INR.

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#### 3.3. Optimized Fractional MPPT

Fractional order control (FOC) was used to overcome the slow dynamic of conventional INR-MPPT. As shown in Figure 5, the DTI is replaced by a discrete fraction PI controller to form the OFMPPT. The FOC "a non-integer order" offers high robustness and design flexibility.

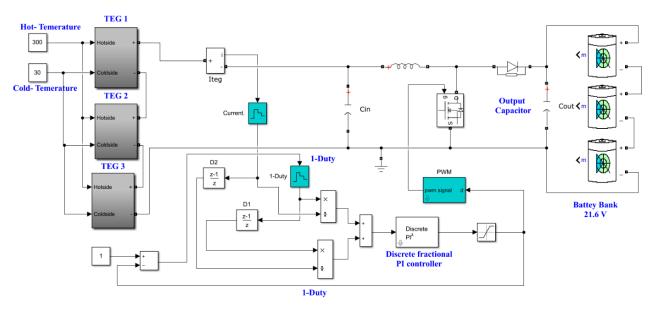


Figure 5. Matlab model of single-sensor OFMPPT.

The fractional PI transfer function can be expressed using the following equation [29]:

$$T_c(s) = k_p + k_I s^{-\lambda} \tag{11}$$

where

 $T_c$  controller transfer function

 $k_I$  is integral gain

 $\lambda$  denotes the fractional order

 $k_p$  is proportional gain

#### 4. Parameters Identification Process of OFMPPT

## 4.1. Objective Function

The proportional and integration gains as well as the fraction order of single-sensor OFMPPT must all be correctly determined. The hunger games search optimization algorithm was used to accomplish this issue. The proportional and integration gains together with fraction order are utilized as decision variables through the optimization process, whereas the energy generated from the TEG is the objective function that needs to be maximized. The objective function problem argument is as follows:

$$f = \underset{x \in R}{\operatorname{argmax}} \left\{ \int_0^t I_{teg}(1 - D) dt \right\}$$
 (12)

where *t* is the simulation time and *x* is the set of input variables.

# 4.2. Hunger Games Search

To express the contraction mode's approaching behavior mathematically, the following relations are suggested [30]:

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$$X(\overrightarrow{t+1}) = \begin{cases} \overrightarrow{X(t)} \cdot (1 + randn(1)), & r_1 < l \\ \overrightarrow{W_1} \cdot \overrightarrow{X_b} + \overrightarrow{R} \cdot \overrightarrow{W_2} \cdot \begin{vmatrix} \overrightarrow{X_b} - \overrightarrow{X(t)} \\ \overrightarrow{X_b} - \overrightarrow{X(t)} \end{vmatrix}, & r_1 > l, r_2 > E \\ \overrightarrow{W_1} \cdot \overrightarrow{X_b} - \overrightarrow{R} \cdot \overrightarrow{W_2} \cdot \begin{vmatrix} \overrightarrow{X_b} - \overrightarrow{X(t)} \\ \overrightarrow{X_b} - \overrightarrow{X(t)} \end{vmatrix}, & r_1 > l, r_2 < E \end{cases}$$
(13)

where  $\overrightarrow{R}$  denotes a random value [-a, a].

 $r_1$  and  $r_2$  are randoms in range between [0, 1].

randn(1) denotes a random number.

t denotes the current iteration.

 $\stackrel{\rightarrow}{W_1}$  and  $\stackrel{\rightarrow}{W_2}$  are the hunger weights.

X(t) is the portion of every particle.

The expression of *E* is presented as in Equation (14).

$$E = \operatorname{sech}(|F(i) - BF|) \tag{14}$$

where  $i \in 1, 2, ..., n$ , F(i) displays each individual's fitness value; BF represents the best fitness

Sech denotes the hyperbolic function  $\left(\operatorname{sech}(x) = \frac{2}{e^x + e^{-x}}\right)$ .

The expression of  $\overrightarrow{R}$  is defined in Equation (15)

$$\overrightarrow{R} = 2 \times a \times rand - a \tag{15}$$

$$a = 2 \times \left(1 - \frac{t}{Max\_iter}\right) \tag{16}$$

where rand denotes a random value

*Max\_iter* is the maximum number of iterations.

The expression of  $\overset{\rightarrow}{W_1}$  and  $\overset{\rightarrow}{W_2}$  are presented in Equations (17) and (18), respectively.

$$W_1(i) = \begin{cases} hungry(i) \cdot \frac{N}{SHungry} \times r_4, r_3 < l \\ 1 & r_3 > l \end{cases}$$
 (17)

The formula of  $\overrightarrow{W_2}$  in Equation (18) is shown as follows:

$$\overrightarrow{W_2(i)} = (1 - exp(-|hungry(i) - SHungry|)) \times r_5 \times 2$$
 (18)

where hungry denotes the hunger of every particle

N denotes the number of particles

SHungry is the sum of hungry feelings of all particles.

 $r_3$ , $r_4$ , and  $r_5$  denote random values.

The expression of hungry(i) is presented below:

$$hungry(i) = \begin{cases} 0, & AllFitness(i) == BF \\ hungry(i) + H, & AllFitness(i)! = BF \end{cases}$$
 (19)

where *AllFitness*(*i*) is the fitness of each individual in the present iteration.

The expression for H is defined as in Equation (20).

$$TH = \frac{F(i) - BF}{WF - BF} \times r_6 \times 2 \times (UB - LB)$$
 (20)

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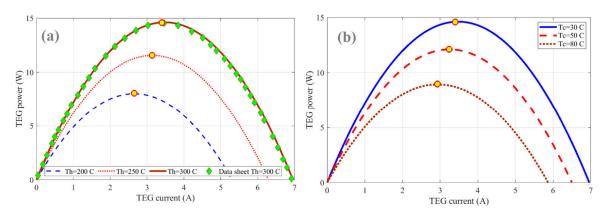
$$H = \begin{cases} LH \times (1+r), & TH < LH \\ TH, & TH \ge LH \end{cases}$$
 (21)

where  $r_6$  is a random number between [0,1]; F(i) denotes the fitness value of every individual. BF denotes the best fitness.

The worst fitness is denoted by *WF*, and the maximum and minimum limits are denoted by *UB* and *LB*, respectively. The hunger sensation H has a lower bound, *LH*.

## 5. Results and Discussion

A Matlab code has been developed to investigate the TEG power as temperature differences change. In the simulations, the type of TEG (TEG1-12611-6.0) is used. The rated current, power, and voltage for a single TEG are 3.4 A, 4.2 V, and 14.6 W, respectively, with cold and hot-side temperatures of 30 and 300 °C, respectively. Figure 6a depicts the power against current of TEG as the hot-side temperature is varied while the cold temperature remains constant at 30 °C. In Figure 6a, Matlab's model data are matched with datasets. Furthermore, the position of the MPP is primarily affected by temperature differences. Figure 6b indicates the power versus current of TEG while maintaining a hot temperature (300 °C) and altering the cold temperature. Every operation state has a unique MPP. To enhance the energy gained from the TEG, the MPPT must constantly follow the MPP, regardless of temperature and/or load demand. Figure 7 depicts the matched load parameters (voltage, power, resistance, and current) as the change in cold and hot temperatures.



**Figure 6.** TEG power against TEG current: (**a**) altering the hot temperature while maintaining cold temperature at 30 C and (**b**) altering cold temperature while maintaining hot temperature at 300 °C.

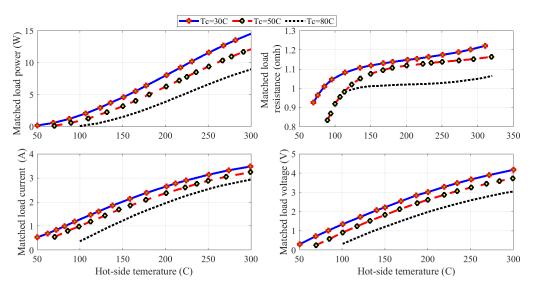


Figure 7. Matched load parameters.

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To define the best paraments of OFMPPT, a hunger games search is used. The maximum number of iterations and the population size are set to 10 and 25, respectively. Throughout the parameter identification process, the objective function presented in (12) is maximized, whereas the unknown parameters of the OFMPPT are used as decision variables. The variation of the objective function during the optimization process is presented in Figure 8. The HGS optimizer needs around 15 iterations to reach the maximum objective function. The optimal values are 0.9, 0.0023, and 0.96, respectively, for the integration gain, proportional gain, and fractional order.

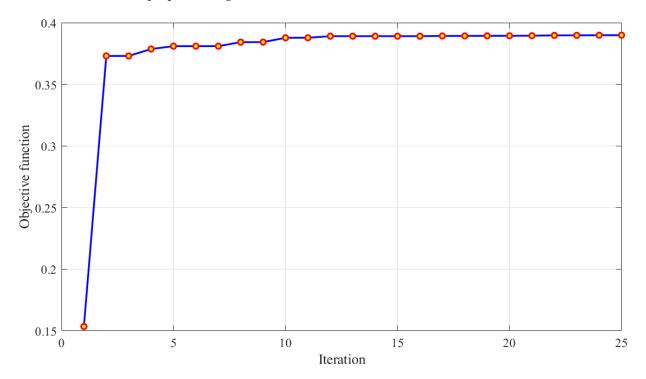


Figure 8. Variation of the objective function.

Once the best parameters for OFMPPT have been determined, the OFMPPT's dynamic and steady state tracking performance is evaluated and compared to INR-MPPT and HC-MPPT. The Matlab TEG power systems for HC-MPPT, INR-MPPT, and OFMPPT are described in Figures 3-5, respectively. The TEG power system consists of three TEG modules (total power 43.8 W), with cold and hot-side temperatures of 300 C and 30 C, respectively. The input inductance and output capacitor are 1 mH and 47 F, respectively, and there are three series batteries (total voltage is 21.6 V). The three MPPTs under consideration are used as a controller to provide a suitable duty cycle to the DC converter. The gain of the discrete integrator is set to 0.8 for the INR-MPPT. Moreover, the parameters of fractional PI for OFMPPT are 0.9, 0.0023, and 0.96 for the integration gain, proportional gain, and fractional order, as defined by HGS. The dynamic response of TEG power for HC-MPPT, INR-MPPT, and OFMPPT is shown in Figure 9. The proposed OFMPPT extracts the maximum power of 43.8 W in 0.07 s with no oscillations around the MPP. Moreover, the INR-MPPT takes approximately 0.33 s to catch the MPP. This means that using OFMPPT reduced tracking time by 78% when compared to INR-MPPT. On the other hand, HC-MPPT reaches the MPP in a short period of time; however, there are significant oscillations around the MPP. This demonstrated the OFMPPT's superiority in tracking the MPP under both dynamic and steady state conditions. The resulting variations in TEG voltage, TEG current, and duty cycle are depicted in Figures 10–12, respectively.

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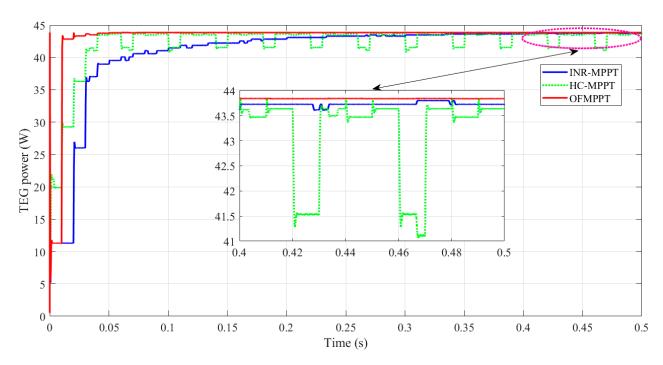


Figure 9. TEG power response during tracking the MPP.

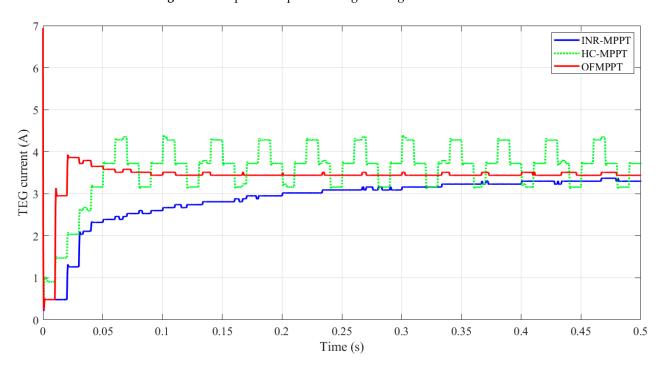


Figure 10. TEG current response while tracking the MPP.

Considering Figure 10, at steady state, the TEG current value using OFMPPT is 3.4 A, which matched with datasheet of TEG1-12611-6.0, as shown in Figure 7.

Considering Figure 11, at steady state, the TEG voltage value using OFMPPT is 12.6 V (4.2 V for each TEG module), which matched with the datasheet of TEG1-12611-6.0, as shown in Figure 7.

Considering Figure 12, at steady state, the duty cycle value using OFMPPT is fixed at 0.52, whereas, using HC-MPPT, there are fluctuations around the MPP.

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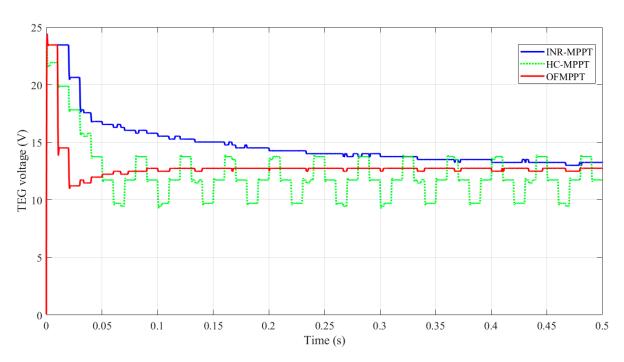


Figure 11. TEG voltage response while tracking the MPP.

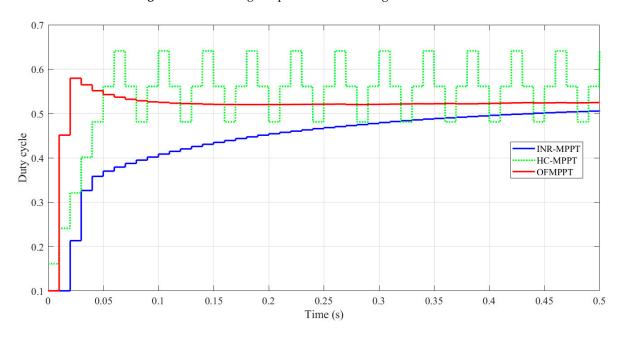


Figure 12. Duty cycle response while tracking the MPP.

## 6. Conclusions

The best parameters for a single-sensor fractional maximum power point tracker for a thermoelectric generator have been identified. This paper accomplishes two major goals: reducing the number of sensors and improving tracking performance. The fractional control is used to improve the dynamic response of incremental resistance (INR-MPPT) and eliminate oscillations around the MPP when using the hill climbing (HC-MPPT) method. Three unknown parameters of optimized fractional (OFMPP); three parameters; proportional gain, integral gain, and fractional order must be correctly identified to ensure an improvement in tracking performance. The hunger games search is used to complete the parameter identification process. During the optimization process, the unknown parameters have been assigned as decision variables, whereas as the objective function is the harvested energy from the TEG. The results confirmed the superiority of OFMPPT

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in both transient and steady state compared to HC-MPPT and INR-MPPT. The proposed OFMPPT succeeded in extracting the maximum power of 43.8 W exactly and very quickly at 0.07 s and no oscillations were recorded around the MPP. Moreover, the INR-MPPT requires about 0.33 s to catch the MPP. This means that, when using OFMPPT, the tracking time decreased by 78% compared to INR-MPPT. On the other hand, HC-MPPT reached the MPP in a short amount time; however, there are high oscillations around the MPP. In future work, the OFMPPT will be used to extract the MPP of the hybrid photovoltaic/TEG system.

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