Reduction of Nonlinear Intersubcarrier Intermixing in Coherent Optical OFDM by a Fast Newton-Based Support Vector Machine Nonlinear Equalizer

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Abstract—A fast Newton-based support vector machine (N-SVM) nonlinear equalizer (NLE) is experimentally demonstrated, for the first time, in 40 Gb/s 16-quadrature amplitude modulated coherent optical orthogonal frequency division multiplexing at 2000 km of transmission. It is shown that N-SVM-NLE extends the optimum launched optical power by 2 dB compared to the benchmark Volterra-based NLE. The performance improvement by N-SVM is due to its ability of tackling both deterministic fiber-induced nonlinear effects and the interaction between nonlinearities and stochastic noises (e.g., polarization-mode dispersion). An N-SVM is more tolerant to intersubcarrier nonlinear crosstalk effects than Volterra-based NLE, especially when applied across all subcarriers simultaneously. In contrast to the conventional SVM, the proposed algorithm is of reduced classifier complexity offering lower computational load and execution time. For a low C-parameter of 4 (a penalty parameter related to complexity), an execution time of 1.6 s is required for N-SVM to effectively mitigate nonlinearities. Compared to conventional SVM, the computational load of N-SVM is \( \sim 6 \) times lower.

Index Terms—Coherent detection, coherent optical OFDM, nonlinearity mitigation, support vector machines.

I. INTRODUCTION

The data rate in an optical transmission system is currently limited by amplified spontaneous emission, which determines the minimum power launched into each fiber span, and the play between chromatic dispersion (CD) and Kerr fiber nonlinearity, which limits the maximum launch power [1].

To increase the data rate of current-generation coherent systems, fiber nonlinearity compensation is required to enable higher launch powers, thereby providing enough optical signal-to-noise ratio to support larger constellation sizes [2]. State-of-the-art fiber nonlinearity compensators (NLC) include digital signal processing (DSP)-based techniques such as digital back-propagation (DBP) [2], [3], reduced complexity Volterra-based nonlinear equalization (NLE) [4], and phase-conjugated twin-waves [5], which tackle nonlinearities of deterministic nature. However, in coherent long-haul optical systems the interaction between nonlinear phenomena with random noises such as polarization-mode dispersion (PMD) results in stochastic nonlinear distortion, which can be partially mitigated using machine learning in the digital domain such as support vectors machines (SVM) [6]–[10].

On the other hand, coherent optical orthogonal frequency division multiplexing (CO-OFDM) is an excellent candidate for long-haul communications because of its high spectral efficiency, flexibility, and tolerance to chromatic dispersion (CD) and PMD. However, due to its high peak-to-average power ratio the deterministic nonlinear cross-talk effects among subcarriers such as inter-subcarrier intermixing (ICI) cross-phase modulation (XPM) and four-wave mixing (FWM) are significantly enhanced causing an additional “stochastic-like” interference [6], [7]. SVM-based NLEs [6]–[10] have shown promising results in CO-OFDM. Nevertheless, since optimization usually requires many steps to converge (in the order of 30) [7], implementation in real-time processing is impractical.

In this paper, we experimentally demonstrate, for the first time, a fast classification SVM-NLE of reduced classifier complexity using the Newton-method (N-SVM) [11] in 16 quadrature amplitude modulated (16-QAM) CO-OFDM at 40 Gb/s, transmitted at 2000 km of standard single-mode fiber (SSMF). It is shown that compared to the benchmark deterministic Volterra-based NLE, N-SVM extends the optimum launched optical power (LOP) by 2 dB with very low DSP computational load and execution time. N-SVM tackles ICI nonlinear crosstalk effects more effectively than Volterra-NLE especially when
applied across all subcarriers simultaneously, rather than on each subcarrier separately.

The paper is organized as follows: Section II analyses the principle of the proposed N-SVM-NLE and the benchmark Volterra-NLE for 16-QAM CO-OFDM. Section III describes the experimental CO-OFDM setup. Section IV presents the experimental results of N-SVM-NLE and Volterra-NLE for CO-OFDM at 2000 km of transmission, and finally in Section V the paper is concluded.

II. PRINCIPLE OF NEWTON SUPPORT VECTOR MACHINE-NLE

A. Operation of N-SVM-NLE for 16-QAM CO-OFDM

In Fig. 1 the block diagram of the CO-OFDM receiver equipped with the N-SVM-NLE is depicted, where the received optical signal is converted back to an electrical one through a homodyne 90° coherent detector. Afterwards, OFDM demodulation process follows similarly to [6], where serial-to-parallel (STP), removal of cyclic prefix (CP) and fast Fourier transform (FFT) are processed. After the FFT block the proposed N-SVM-NLE takes place for all subcarriers simultaneously before decoding and parallel-to-serial (PTS) conversion. The proposed N-SVM-NLE implements a fast Newton method that suppresses decoding and parallel-to-serial (PTS) conversion. The proposed N-SVM-NLE takes place for all subcarriers simultaneously before decoding and parallel-to-serial (PTS) conversion. The proposed N-SVM-NLE implements a fast Newton method that suppresses decoding and parallel-to-serial (PTS) conversion. The proposed N-SVM-NLE implements a fast Newton method that suppresses decoding and parallel-to-serial (PTS) conversion. The proposed N-SVM-NLE implements a fast Newton method that suppresses decoding and parallel-to-serial (PTS) conversion.
The SVM formulation of (3) is rewritten by (4) into the objective function where

\[ \min f(w, b) = \left( \frac{1}{2} \right) u^T u + \left( \frac{C}{2} \right) \| [e - DH u]_+ \|^2 \]  

\[ (4) \]

**B. The “Stepless” N-SVMA Algorithm**

The adopted N-SVM process is described in Fig. 3 showing the finite “stepless” Newton method which solves the strongly convex unconstrained minimization problem in (4). In most of tested cases [11]–[14] this algorithm has given an optimum solution with a few number of iterations varying from 5 to 8.

**III. BENCHMARK VOLterra-NLE FOR 16-QAM CO-OFDM**

The adopted Volterra-NLE is similar to [4], accounting for single-band and single-polarization as depicted in Fig. 4. It employs the inverse Volterra-series transfer function (IVSTF) with up to 3rd order Volterra kernels. It should be noted that when higher-order kernels were employed, similar results were revealed [15]. IVSTF-NLE offers \( \sim 25\% \) reduced complexity compared to full-step/span DBP [4], [9] and inherits some of the features of the hybrid time-and-frequency domain implementation, such as non-frequency aliasing and simple implementation.

The process of nonlinearity compensation by Volterra-NLE is described as follows: The input OFDM signal is first converted to frequency domain by FFT. The Volterra-NLE compensates CD using a linear compensator.

On the other hand, the number of required nonlinear compensators depends on the number of homogeneous spans in the transmission link. The output of the linear and nonlinear compensator is combined and converted back to time-domain using the inverse FFT (IFFT). The Volterra-NLE procedure can be described from (5)–(9). Since a reduced complexity 3rd order IVSTF is considered, the kernels \( H_1(\omega, z) \) and \( H_3(\omega_1, \omega_2, \omega - \omega_1 + \omega_2, z) \) are given by

\[ H_3(\omega_2) = e^{-\alpha z/2} e^{-j\omega^2 \beta z/2} \]  

\[ (5) \]

\[ H_3(\omega_1, \omega_2, \omega - \omega_1 + \omega_2, z) = -j\gamma \frac{H_1(\omega, z)}{4\pi^2} \times \frac{1 - e^{-(\alpha + j\beta)z}}{\alpha + j\beta(\omega_1 - \omega)(\omega_1 - \omega_2)} \]  

\[ (6) \]

where \( \omega \) is the optical frequency and \( \omega_1, \omega_2 \) are the dummy variables acting as parameters and influence the interactions of the lightwaves at different frequency, especially the ICI interaction effects. \( \alpha \) is the fiber loss, \( \beta \) is the 2nd order CD parameter and \( \gamma \) accounts for the effect of fiber nonlinearity averaging. For an optically amplified Nspan fiber link with Lspan being the span length, the corresponding \( \beta^L \) inverses given by the nonlinear kernels as

\[ K_1(\omega) = H_1^{-1}(\omega) = e^{-j\omega^2 \beta L_{\text{span}} / 2} \]  

\[ (7) \]

\[ K_3(\omega_1, \omega_2, \omega - \omega_1 + \omega_2) = -j\gamma \frac{N_{\text{span}}}{4\pi^2} K_1(\omega) \times \frac{1 - e^{-(\alpha + j\beta)\Delta \omega}}{\alpha + j\beta(\omega_1 - \omega)(\omega_1 - \omega_2)} \sum_{k=1}^{N_{\text{span}}} e^{-jk\beta L_{\text{span}} \Delta \omega} \]  

\[ (8) \]

\[ \approx -j\gamma \frac{N_{\text{span}}}{2\pi^2} \sum_{k=1}^{N_{\text{span}}} e^{-jk\beta L_{\text{span}} \Delta \omega}. \]  

\[ (9) \]

The corresponding compensation scheme representing (7) and (9) is applied in Fig. 4. Each nonlinear compensation stage is a realization of

\[ K_3(\omega_1, \omega_2, \omega - \omega_1 + \omega_2) \approx -j\gamma \frac{1 - e^{-\alpha L_{\text{span}}}}{\alpha} \times K_1(\omega) e^{-jk\beta L_{\text{span}} \Delta \omega}. \]  

\[ (10) \]

Finally, since single-polarization is considered we have

\[ S_{K_1}(\omega) \int_{-\infty}^{\infty} K_3, K_1(\omega_1, \omega_2, \omega - \omega_1 + \omega_2) \times A(\omega_1) A^{*}(\omega_2) \times A(\omega - \omega_1 + \omega_2) d\omega_1 d\omega_2 \]  

\[ (11) \]
where $S_{K_1}(\omega)$ is derived by passing the received signal through $\langle H_{CD}(K_1, K_2) \rangle$, and nonlinearity compensation is performed by $j k(|.|^2)$ where we multipy the received signal by a constant $k$ related to the nonlinear distortion and the total power. This parameter varies for this configuration and is obtained by sweeping it to get optimum performance, which is part of the calibration of the Volterra-NLE. Finally, the residual CD is compensated passing through $\langle H_{CD} \rangle^{-1}(K_1, K_2)$.

**IV. EXPERIMENTAL SETUP**

Fig. 5 depicts the experimental setup where an external cavity laser (ECL) of 100 kHz linewidth was modulated using a dual-parallel Mach-Zehnder modulator (DP-MZM) in IQ configuration. The DP-MZM was fed with OFDM I-Q components, which was generated offline. The transmission path at 1550.2 nm was a recirculating loop consisting of $20 \times 100$ km spans of Sterlite OH-LITE (E) SSMF (attenuation of 18.9–19.5 dB/100 km) controlled by acousto-optic modulator (AOM). The loop switch was located in the mid-stage of the 1st Erbium-doped fiber amplifier (EDFA) and a gain-flattening filter (GFF) was placed in the mid-stage of the 3rd EDFA. The optimum LOP was swept by controlling the output power of the EDFAs. At the receiver, the incoming signal was combined with another 100 kHz linewidth ECL acting as local oscillator. After downconversion, the baseband signal was sampled using a real-time oscilloscope operating at 80 GS/s and processed offline in MATLAB. 400 OFDM symbols were generated using a 512-point IFFT in which 210 subcarriers were modulated using 16-QAM. To eliminate inter-symbol-interference from linear effects, a CP of 2% was included. For fair comparison among linear equalization (LE), Volterra-NLE and the proposed N-SVM-NLE, the net and raw bit-rate were fixed at $\sim$40 Gb/s and $\sim$46 Gb/s, respectively. The N-SVM training overhead was set at 10% (optimum value for LE) resulting in a training length of 40 symbols. The offline OFDM demodulator included timing synchronization, frequency offset compensation, channel estimation and equalization with the assistance of an initial training sequence, as well as I-Q imbalance and CD compensation using an overlapped frequency domain equalizer employing the overlap-and-save method. When N-SVM-NLE was performed, the LE was neglected due to N-SVM ability of compensating both linear and nonlinear inter-subcarrier crosstalk effects. The CO-OFDM transceiver and transmission parameters are depicted on Table I.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Net bit-rate (LE, NLEs)</td>
<td>$\sim$40 Gb/s</td>
</tr>
<tr>
<td>Raw bit-rate (LE, NLEs)</td>
<td>$\sim$46 Gb/s</td>
</tr>
<tr>
<td>Signal modulation format</td>
<td>16-QAM</td>
</tr>
<tr>
<td>OFDM symbols</td>
<td>400</td>
</tr>
<tr>
<td>Modulated OFDM subcarriers</td>
<td>210</td>
</tr>
<tr>
<td>Cyclic prefix (CP) length</td>
<td>2%</td>
</tr>
<tr>
<td>FFT/IFFT size</td>
<td>512</td>
</tr>
<tr>
<td>N-SVM Training overhead</td>
<td>10%</td>
</tr>
<tr>
<td>N-SVM Training symbol length</td>
<td>40 symbols</td>
</tr>
<tr>
<td>ECL linewidth</td>
<td>100 KHz</td>
</tr>
<tr>
<td>OH-LITE (E) SSMF attenuation</td>
<td>18.9–19.5 dB/100 km</td>
</tr>
<tr>
<td>Span number</td>
<td>20</td>
</tr>
<tr>
<td>Span length</td>
<td>100 km</td>
</tr>
<tr>
<td>Transmission wavelength</td>
<td>1550.2 nm</td>
</tr>
</tbody>
</table>

**V. RESULTS AND DISCUSSION**

In Fig. 6 the Q-factor against the training overhead of N-SVM-NLE is depicted for 16-QAM CO-OFDM at 2000 km of transmission for a LOP of 2 dBm, which is the optimum LOP of LE. It should be noted that changing the training overhead, the raw bit-rate was adjusted accordingly. From Fig. 6 it is evident that a minimum 10% of training data is required for N-SVM-NLE to effectively tackle the OFDM inter-subcarrier crosstalk effects (e.g. ICI-XPM/FWM). In this paper, 10% of training data are employed for N-SVM-NLE in all sections.

In Fig. 7, the Q-factor against the LOP is plotted for the 40 Gb/s CO-OFDM system at 2000 km of transmission for LE, Volterra-NLE, and N-SVM-NLE. It is shown that compared to Volterra-NLE, the proposed N-SVM-NLE can extend the
optimum LOP by 2 dB (FEC-limit at $\sim$9.8 dB), while in comparison to LE it can extend the LOP by $\sim$3.5 dB. To corroborate the N-SVM-NLE performance enhancement, Fig. 8 is plotted, showing the received 16-QAM constellations diagrams for the three types of equalization and without equalization at 6 dBm of LOP.

In Fig. 9, the Q-factor against the $C$-parameter (the $C$ value from (2)) is plotted for the CO-OFDM system under test at a LOP of 4 dBm. The $C$-parameter (also called “penalty parameter”) is related to the computational complexity of N-SVM. It is shown that a $C$ of only 4 is required at an execution time of 1.6 sec for stable optimum performance. This time required by the training process is considered for a general-purpose CPU operating at 1.2 GHz. However, this time will be drastically reduced in implementations based on Field-Programmable Gate-Array or Application Specific Integrated Circuits. The minimum required $C$ value for N-SVM-NLE is $\sim$6 times less than the corresponding “penalty parameter” of the conventional SVM-NLE reported in [7] for 16-QAM CO-OFDM. This occurs because i) N-SVM performs fast classification tasks that separate cases of different class labels, and ii) the conventional SVM performs both classification and regression analysis in contrast to N-SVM which only classifies the data. It should be noted that a transmission performance comparison between the proposed N-SVM and the conventional SVM [7] is out of the scope of this paper since fair comparison is not feasible.

In Fig. 10 the impact of N-SVM on the nonlinear ICI crosstalk effects is investigated for the adopted CO-OFDM system. A comparison is also made with the benchmark Volterra-NLE to evaluate the impact of stochastic nonlinearities. In Fig. 10, an additional case for exploring the nonlinear phenomena in OFDM is proposed, in which the NLEs under test are performed for each subcarrier. Although this case is unrealistic since it substitutes a separate NLE for each subcarrier, it will provide a holistic and deeper understanding on the physics underlying nonlinear phenomena in CO-OFDM. In Fig. 11, a conceptual diagram is depicted for the application of NLE, and NLE per subcarrier (related to Volterra and N-SVM) on received OFDM signal. N-SVM and Volterra NLEs ‘per subcarrier’ cases (the dotted lines in Fig. 10) includes 210 NLEs in contrast to the realistic case where 1 NLE process all subcarriers together. In Fig. 10, it is shown that in comparison to the ‘per subcarrier’
case, when N-SVM is applied across all subcarriers it reduces the fiber nonlinearity penalty by 0.5 dB. This occurs because when applying N-SVM on each subcarrier separately, ICI nonlinear crosstalk effects are not combated. Finally, it is confirmed that CO-OFDM is influenced by stochastic nonlinearities which cannot be tackled by the deterministic Volterra-NLE.

The results from Fig. 10 indicate that the adopted realistic N-SVM-NLE which accounts for all subcarriers together, provides effective and fast compensation of inter-subcarrier nonlinear crosstalk effects in CO-OFDM.

VI. CONCLUSION

A novel fast N-SVM-NLE of reduced classifier complexity was experimentally demonstrated in 40 Gb/s 16-QAM CO-OFDM at 2000 km of SSMF. In comparison to Volterra-NLE, the proposed N-SVM extended the optimum LOP by 2 dB with very low computational load and execution time. N-SVM tackled inter-subcarrier nonlinear crosstalk effects more effectively than Volterra-NLE especially when applied across all subcarriers simultaneously.

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REFERENCES


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Nick J. Doran has more than 30-years research experience in high-speed and long distance optical communications. He led a research team at British Telecom (BT) for 10 years on both theoretical and experimental investigations in ultrahigh speed optical systems from 1981 to 1991. He jointly established the photonics research group at Aston University, from 1991 to 2000, specializing in soliton communication and processing. During this time the research was extensively funded by EPSRC and supported by industrial contracts with Marconi and KDD. In 2000, he established a startup development within Marconi (SOLSTIS) to develop an ultralong communication system based on his research. In 2005, he took on the role of Head and Director of the Institute of Advanced Telecommunication, Swansea University. He returned to Aston University in November 2013 and there runs two key research projects on nonlinear fibre amplification (EPSRC) Wideband Optical Communication Systems Using Phase-Sensitive/Insensitive Fiber Parametric Amplifiers and optical networks (FP7 DISCUS). Prof. Doran has published more than 200 papers and 20 patents on optical transmission and processing. He invented the concept of dispersion managed solitons and the extensively used Nonlinear Optical Loop Mirror. He has a current H-index of 48 with more than 8300 citations of his publications.

Andrew D. Ellis has previously worked for British Telecom Research Laboratories as a Senior Research Engineer investigating the use of optical amplifiers and advanced modulation formats in optical networks and for the Corning Research Centre as a Senior Research Fellow where he led activities in optical component characterization. From 2003, he headed the Transmission and Sensors Group, Tyndall National Institute, Cork, Ireland, where he was also a member of the Department of Physics, University College Cork. His research interests include the evolution of core and metro networks, and the application of photonics to sensing. He is currently a Professor of optical communications at Aston University, Birmingham, U.K., where he is also Deputy Director of the Institute of Photonics Technologies. He has published more than 170 journal papers and more than 25 patents in the field of photonics, primarily targeted at increasing capacity, reach and functionality in the optical layer. Prof. Ellis is a member of the Institute of Physics and the Institute of Engineering Technology, and is a Chartered Physicist. He is an Associate Editor of the journal Optics Express. He is a member of the Technical Program Committee of ECOC, chairing sub-committee three devoted to digital and optical signal processing in 2014.